中国科学院数学与系统科学研究院 Academy of Mathematics and Systems Science, CAS

图论组合与网络研究中心

Center for Graph Theory, Combinatorics and Networks



Turán theorems for even cycles in random 题目:

hypergraph

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时 间: 5月21日(星期二) 15:00-16:00

地 点: 数学院南楼 N620

摘 要:

Let \mathcal{F} be an r-uniform hypergraph. The random Turán number $\operatorname{ex}(G^r_{n,p},\mathcal{F})$ is the maximum number of edges in an \mathcal{F} -free subgraph of $G^r_{n,p}$, where $G^r_{n,p}$ is the Erdős-Rényi random r-graph with parameter p. Let C^r_ℓ denote the r-uniform linear cycle of length ℓ . For $p \geq n^{-r+2+o(1)}$, Mubayi and Yepremyan showed that $\operatorname{ex}(G^r_{n,p},C^r_{2\ell}) \leq \max\{p^{\frac{1}{2\ell-1}}n^{1+\frac{r-1}{2\ell-1}+o(1)},pn^{r-1+o(1)}\}$. This upper bound is not tight when $p \leq n^{-r+2+\frac{1}{2\ell-2}+o(1)}$. Recently, we close the gap for $r \geq 4$. More precisely, we show that $\operatorname{ex}(G^r_{n,p},C^r_{2\ell}) = \Theta(pn^{r-1})$ when $p \geq n^{-r+2+\frac{1}{2\ell-1}+o(1)}$. Similar results have recently been obtained independently in a different way by Mubayi and Yepremyan. For r=3, we significantly improve Mubayi and Yepremyan's upper bound.

报告人简介: 聂家熹,复旦大学上海数学中心博士后,导师为吴河辉教授。2022年于加州大学圣地亚哥分校(University of California, San Diego)获得数学博士学位,导师为Jacques Verstraëte 教授。2016年本科毕业于南开大学数学伯苓班。主要研究兴趣为极值组合,包括 Ramsey问题,Turán问题,图分解问题等。目前已在J. Combin. Theory Ser. B,Random Structures Algorithms, SIAM J. Discrete Math, J. Graph Theory, European J. Combin.等期刊发表多篇论文。